

*Robust Failure Diagnosis of Discrete Event Systems
and Its Applications*

João Carlos Basilio

***Workshop on Analysis and Control for Resilience
of Discrete Event Systems***



UNIVERSIDADE FEDERAL
DO RIO DE JANEIRO



Talk outline

- 1. Fault Diagnosis and Robustness*
- 2. Fault Diagnosis of Discrete-Event Systems*
- 3. Online Diagnosis*
- 4. Robust Fault Diagnosis of Discrete-Event Systems. Why?*
- 5. Robust Diagnosis against intermittent loss of observation*
- 6. Diagnosability of Networked DES*
- 7. Conclusion*

I. Fault Diagnosis and Robustness

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Fault occurrences must be diagnosed ASAP

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 - ▶ It is performed online
- ▶ **Fault Diagnosability:** is a system property that ensures that the fault can be diagnosed
 - ▶ It is performed offline
 - ▶ It requires the knowledge of a model of the system

Robustness

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**How to bring robustness to
Fault Diagnosis of Discrete-Event Systems?**

II. Fault Diagnosis of Discrete-Event Systems

Discrete-Event Systems

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Discrete-Event Systems

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- ▶ DES are event dependent \Rightarrow Better described with languages
- ▶ Automaton is one of the modeling formalisms

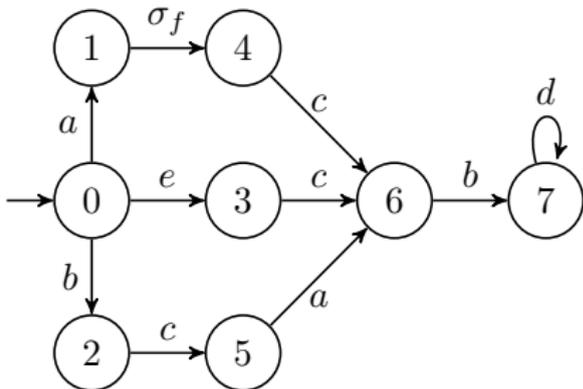
$$G = (X, \Sigma, \delta, x_0)$$

- ▶ Kleene-closure of Σ : Σ^*
- ▶ Language generated by G :
 $L(G) = \{s \in \Sigma^* : (\exists x \in X)[\delta(x_0, s) = x]\}$

Language diagnosability

$$G = (X, \Sigma, \delta, x_0)$$

- ▶ $X = \{0, 1, 2, 3, 4, 5, 6, 7\}$
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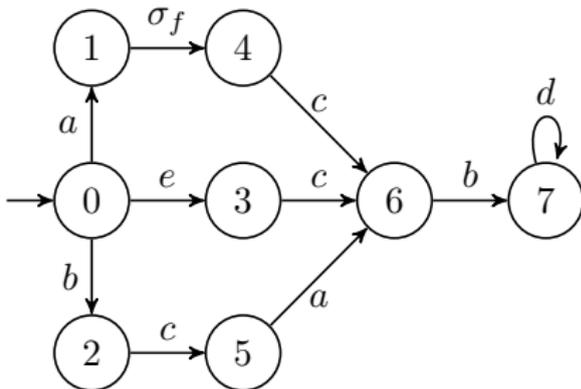


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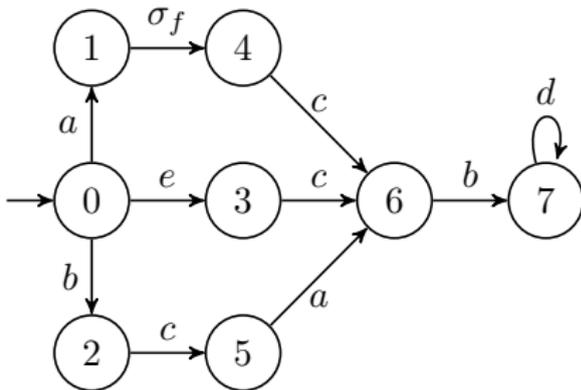
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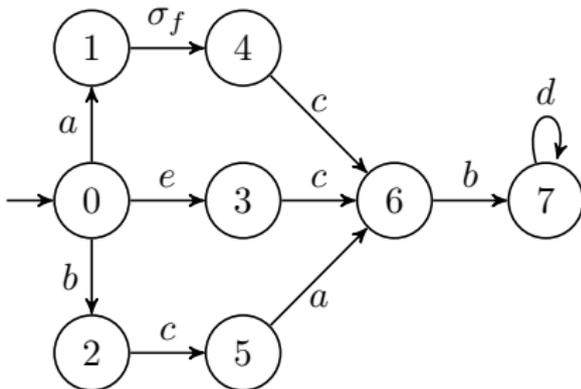
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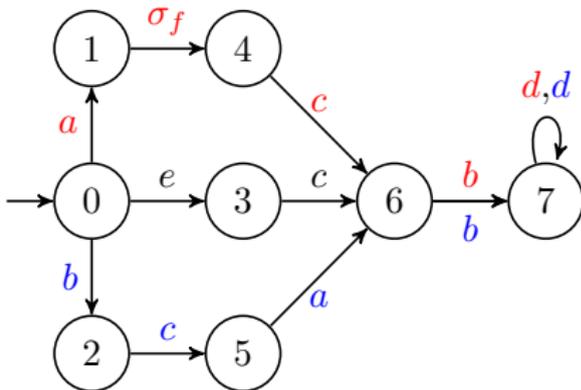
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$$s_Y = a\sigma_fcbd^n, s_N = bcabd^n$$

$$\Downarrow$$

$$P_{\Sigma, \Sigma_o}(s_Y) = P_{\Sigma, \Sigma_o}(s_N) = cd^n$$



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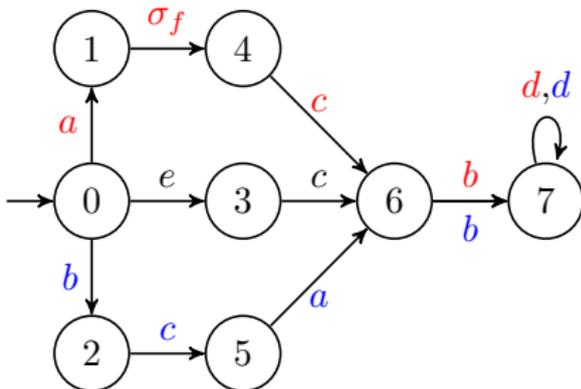
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- ▶ **$L(G)$ not diagnosable**



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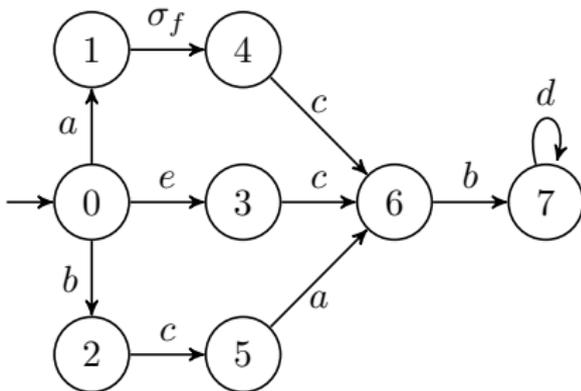
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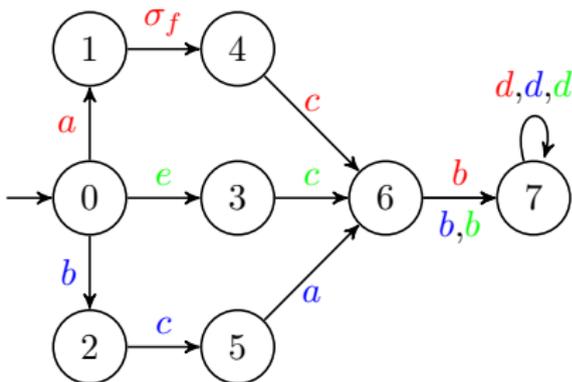
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- ▶ $s_Y = a\sigma_fcbd^n \Rightarrow P_{\Sigma, \Sigma_o}(s_Y) = bd^n$

- ▶ $s'_N = bcabd^n \Rightarrow P_{\Sigma, \Sigma_o}(s'_N) = bbd^n$

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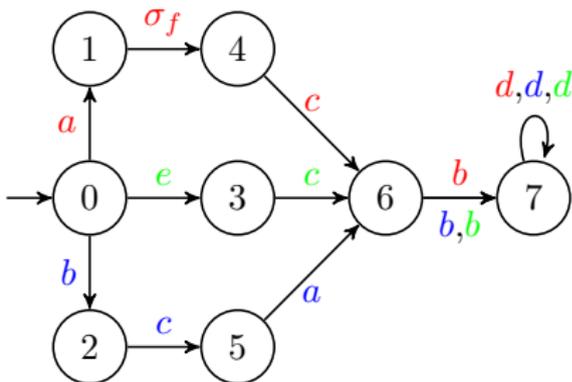
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- ▶ **$L(G)$ diagnosable**



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- ▶ Language $L(G)$, is diagnosable with respect to projection P_{Σ, Σ_o} and $\Sigma_f = \{\sigma_f\}$ if the following holds true:

$$(\exists n \in \mathbb{N})(\forall s \in \Psi(\Sigma_f))(\forall t \in L/s)(\|t\| \geq n \Rightarrow D),$$

where the diagnosability condition D is

$$(\forall \omega \in P_{\Sigma, \Sigma_o}^{-1}(P_{\Sigma, \Sigma_o}(st)) \cap L)(\Sigma_f \in \omega),$$

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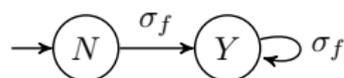
III. Online Diagnosis

Diagnoser Automaton

- ▶ $G = (X, \Sigma, \delta, x_0)$: system automaton whose language is diagnosable with respect to P_{Σ, Σ_o} and σ_f

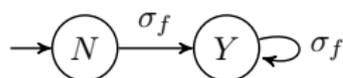
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Diagnoser Automaton

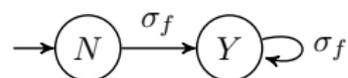
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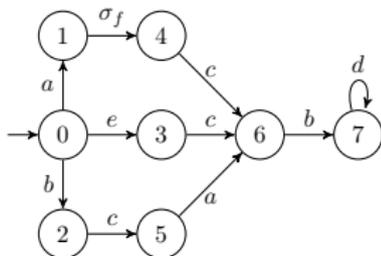
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- ▶ **Labeled automaton:** $G_\ell = G \parallel A_\ell$
- ▶ **Diagnoser:** $G_d(\Sigma_o) = \text{Obs}(G_\ell, \Sigma_o) = (X_d, \Sigma_o, \delta_d, x_{0,d})$

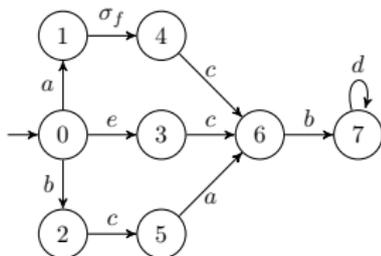
Diagnoser Automaton - Example

► System Automaton G

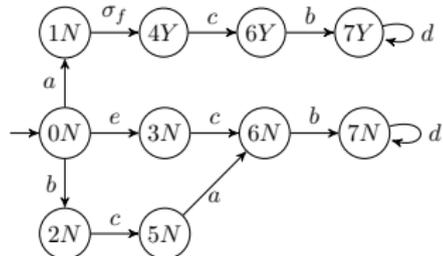


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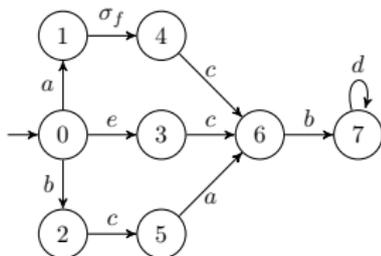


► Labeled Automaton G_ℓ

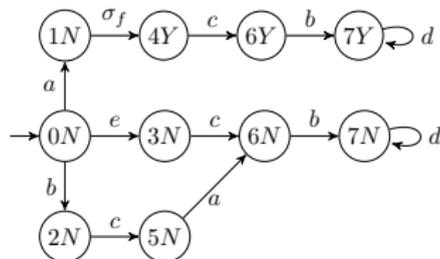


Diagnoser Automaton - Example

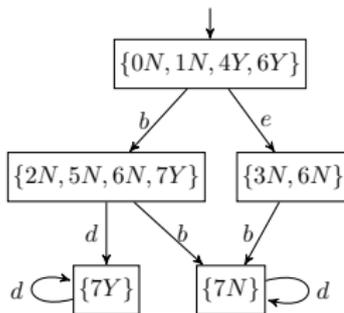
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► Labeled Automaton G_ℓ



► Diagnoser Automaton G_d ($\Sigma_o = \{b, d, e\}$)

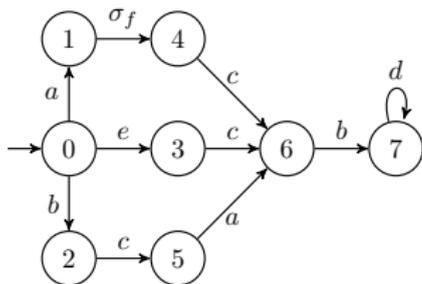


*IV. Robust Fault Diagnosis of Discrete-Event
Systems. Why?*



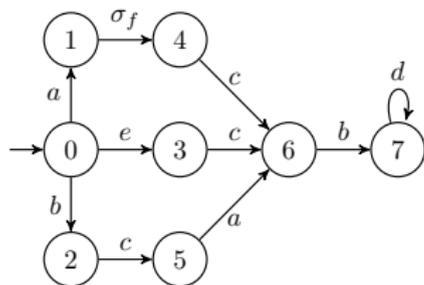
Motivation Example: loss of event observation

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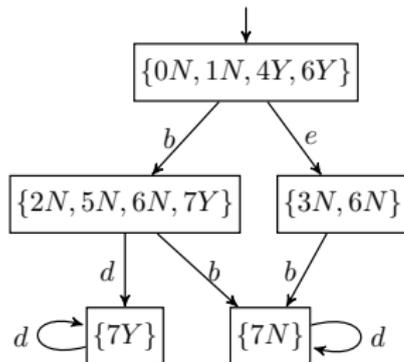


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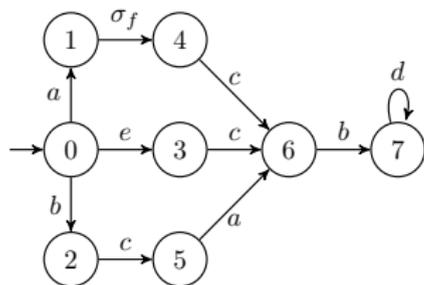


► Diagnoser G_d ($\Sigma_o = \{b, d, e\}$)

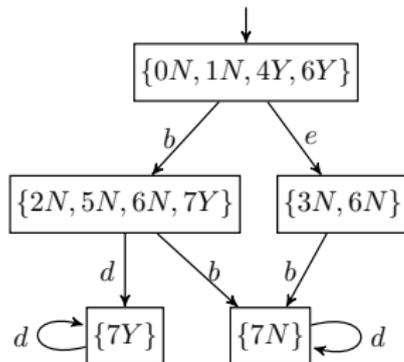


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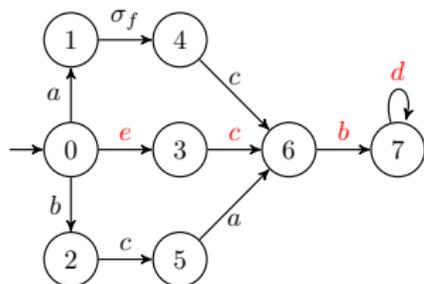
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What would happen if, for some reason, the occurrence of event e did not reach G_d ?

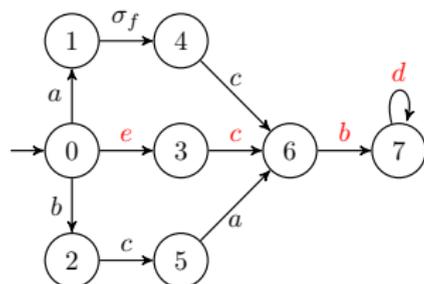
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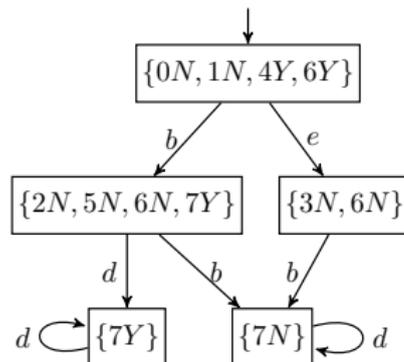


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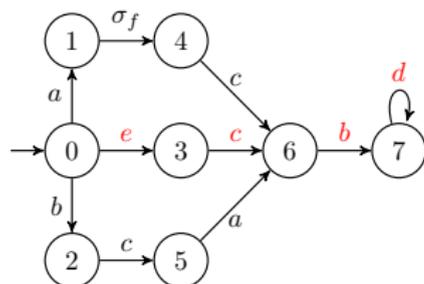


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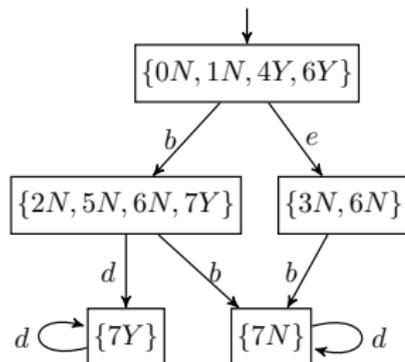


Motivation Example: loss of event observation

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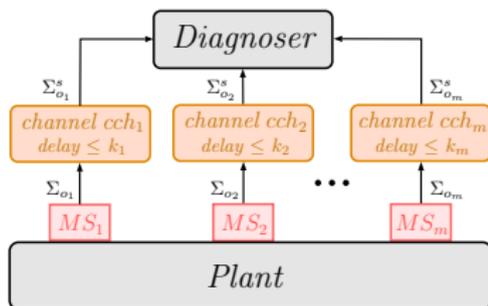
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**Diagnoser would end up in state $\{7Y\}$
FALSE POSITIVE**

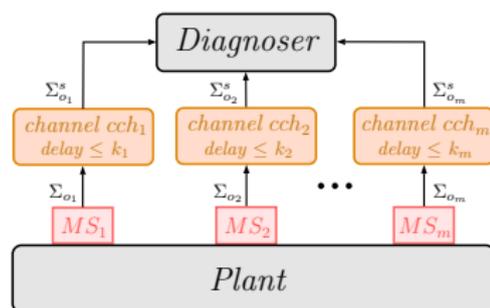
Motivation Example: Networked DES

► Networked



Motivation Example: Networked DES

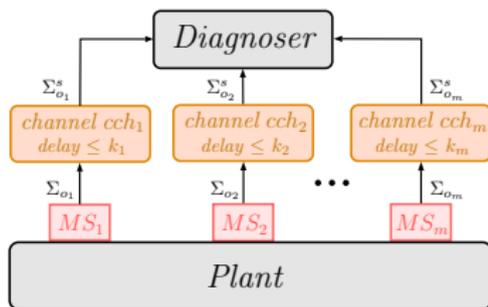
► Networked



- Measurement sites: MS_i , $i = 1, 2, \dots, m$
- Communication channels: cch_i , $i = 1, 2, \dots, m$
- Communication channels delays: k_i , $i = 1, 2, \dots, m$ Steps

Motivation Example: Networked DES

► Networked



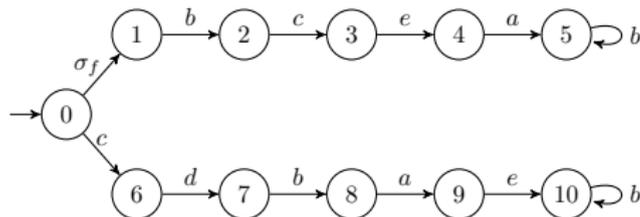
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Event observation can be performed in an order different from the actual event occurrences due to different delays of the various communication channels employed.

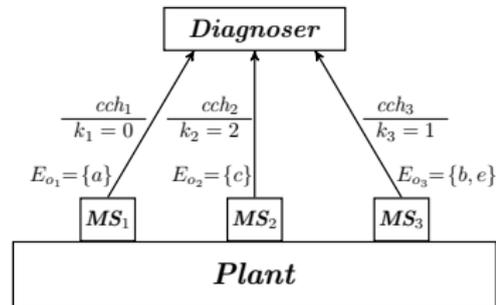
Motivation Example: Networked DES

▶ Automaton



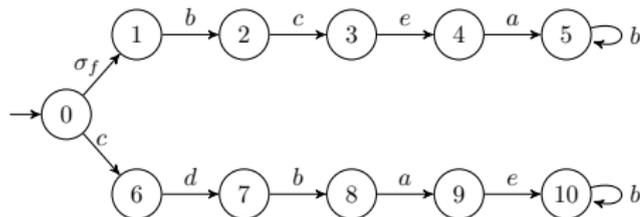
▶ $\Sigma = \{a, b, c, d, e, \sigma_f\}$, $\Sigma_f = \{\sigma_f\}$

▶ Networked DES



Motivation Example: Networked DES

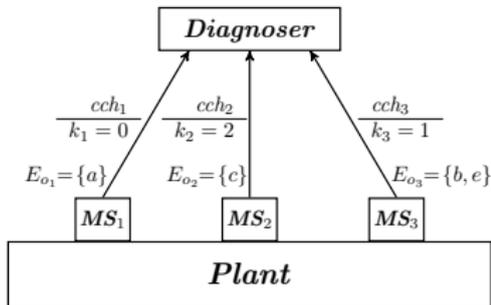
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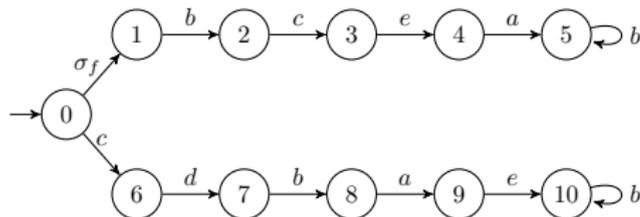
- ▶ Diagnosable if no delay exists

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Motivation Example: Networked DES

▶ Automaton



▶ $\Sigma = \{a, b, c, d, e, \sigma_f\}$, $\Sigma_f = \{\sigma_f\}$

▶ Diagnosable if no delay exists

▶ Assuming there are communication channel delays:

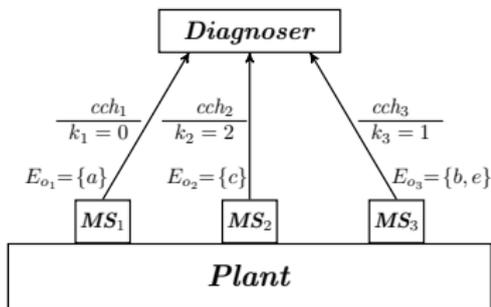
▶ $s_Y = \sigma_f bceab^n$ and $s_N = cdbaeb^n$, $n \in \mathbb{Z}_+$

▶ $s_{Y_a} = \sigma_f bcc_s b_s eaa_s e_s (bb_s)^n$, $s_{N_a} = cc_s dbb_s aa_s ee_s (bb_s)^n$

▶ $P_{\Sigma_a, \Sigma_0^s}(s_{Y_a}) = P_{\Sigma_a, \Sigma_0^s}(s_{N_a}) = c_s b_s a_s e_s (b_s)^n$

▶ Non diagnosable

▶ Networked DES



V. Robust Diagnosis against intermittent loss of observation

Key to the Solution: Language augmentation

► Dilation (Carvalho et al., 2014)

► $\Sigma_o = \Sigma_{ilo} \dot{\cup} \Sigma_{nilo}$

Σ_{ilo} : subset of Σ_o whose events are subject to intermittent loss of observations

Σ_{nilo} : set of events whose observations are never lost.

► $\Sigma'_{ilo} = \{\sigma' : \sigma \in \Sigma_{ilo}\}$

► $\Sigma_{dil} = \Sigma \cup \Sigma'_{ilo}$

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$$\text{► } \Sigma_{dil} = \Sigma \cup \Sigma'_{ilo}$$

► The dilation D is the mapping

$$D : \Sigma \rightarrow 2^{\Sigma_{dil}}$$

$$\sigma \mapsto D(\sigma) = \begin{cases} \{\sigma\}, & \sigma \in \Sigma \setminus \Sigma_{ilo}, \\ \{\sigma, \sigma'\}, & \sigma \in \Sigma_{ilo}, \end{cases}$$

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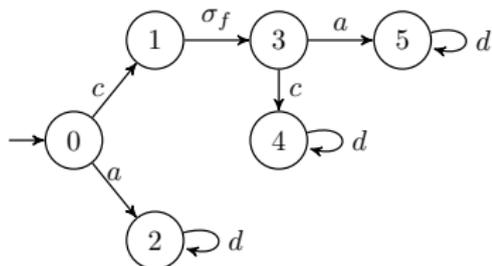
$$\sigma \mapsto D(\sigma) = \begin{cases} \{\sigma\}, & \sigma \in \Sigma \setminus \Sigma_{ilo}, \\ \{\sigma, \sigma'\}, & \sigma \in \Sigma_{ilo}, \end{cases}$$

► Extension to languages:

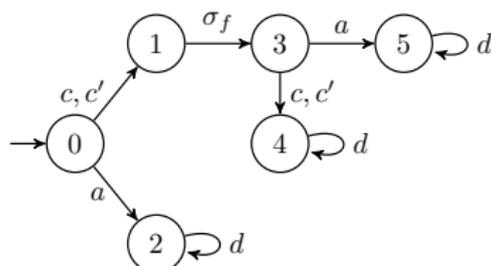
$D(\varepsilon) = \varepsilon$, and $D(s\sigma) = D(s)D(\sigma)$, for $s \in \Sigma^*$ and $\sigma \in \Sigma$.

Dilation - Example

▶ Automaton G



▶ Dilated automaton G_{dil}



- ▶ $\Sigma = \{a, b, c, d, \sigma_f\}$, $\Sigma_o = \{a, b, c, d\}$, $\Sigma_f = \{\sigma_f\}$
- ▶ $L(G) = pre(c\sigma_f(a + c)d^* + ad^*)$
- ▶ $\Sigma_{ilo} = \{c\}$
- ▶ $L(G) = pre((c + c')\sigma_f(a + c + c')d^* + ad^*)$

Robust diagnosability



Diagnosability requires that there do NOT exist AMBIGUOUS SEQUENCES

Robust diagnosability



Diagnosability requires that there do NOT exist AMBIGUOUS SEQUENCES

- ▶ **Definition:** Language $L(G)$ is robustly diagnosable with respect to dilation D , projection $P_{\Sigma_{dil}, \Sigma_o} : \Sigma_{dil}^* \rightarrow \Sigma_o^*$ and $\Sigma_f = \{\sigma_f\}$ if the following holds true:

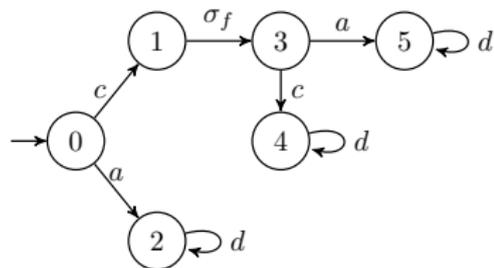
$$(\exists n \in \mathbb{N})(\forall s \in \Psi(\Sigma_f))(\forall t \in L/s)(\|t\| \geq n \Rightarrow R_D),$$

where the robust diagnosability condition R_D is

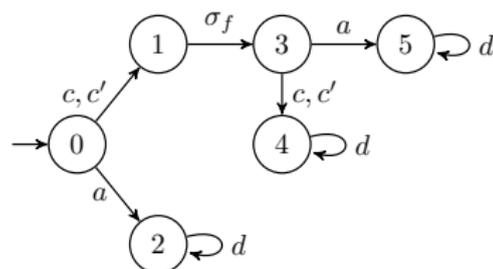
$$(\nexists \omega \in L) [P_{\Sigma_{dil}, \Sigma_o}(D(st)) \cap P_{\Sigma_{dil}, \Sigma_o}(D(\omega)) \neq \emptyset \wedge (\Sigma_f \notin \omega)].$$

Robust Diagnosability - Example

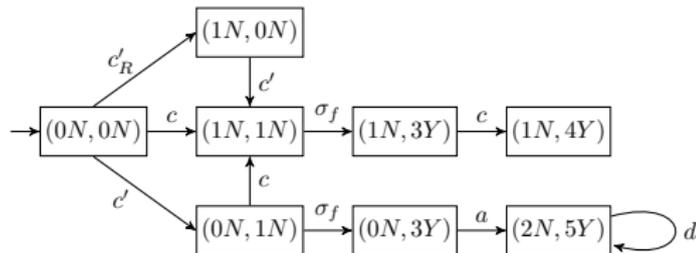
▶ Automaton G



▶ Dilated automaton G_{dil}

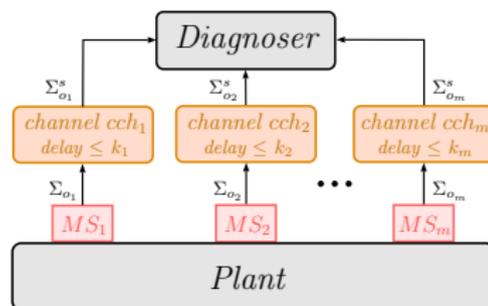


▶ Robust Diagnosability verification



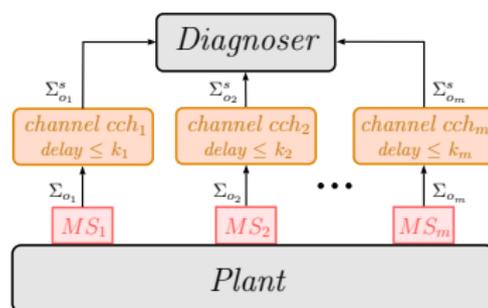
VI. Diagnosability of Networked DES

Networked DES



- ▶ Automaton:
 $G = (X, \Sigma, \delta, x_0)$
- ▶ Measurement sites:
 $MS_i, i = 1, \dots, m$
- ▶ Channel delay structure:
 $\vec{k} = [k_1 \quad k_2 \quad \dots \quad k_m]$

Networked DES



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 $G = (X, \Sigma, \delta, x_0)$
- ▶ Measurement sites:
 $MS_i, i = 1, \dots, m$
- ▶ Channel delay structure:
 $\vec{k} = [k_1 \quad k_2 \quad \dots \quad k_m]$

- ▶ Event occurrences and observations must be distinguished

$$\Sigma_{o_i}^s = \{\sigma_s : \sigma \in \Sigma_{o_i}\} \rightarrow \Sigma_o^s = \bigcup_{i=1}^m \Sigma_{o_i}^s$$

- ▶ Augmented event set

$$\Sigma_a = \Sigma \cup \Sigma_o^s$$

- ▶ Observation of system evolution

$$P_{\Sigma_a, \Sigma_o^s} : \Sigma_a^* \rightarrow \Sigma_o^{s*}$$

Language augmentation (Nunes et al, 2018)

$$\chi : \Sigma^* \rightarrow 2^{\Sigma_a^*}$$

$$s \mapsto \chi(s) = \{s_a \in \Sigma_a^* : (s_a \models \mathbf{C1}) \wedge (s_a \models \mathbf{C2}) \wedge (s_a \models \mathbf{C3})\}$$

- ▶ **C1.** $P_{\Sigma_a, \Sigma}(s_a) = s$;
- ▶ **C2.** For all $\sigma \in \Sigma_{o,i}$, if $\sigma_s^{(p)} \in s_a$, then:

$$\|P_{\Sigma_a, \Sigma_{o_i}^s}(pre(s_a, \sigma_s^{(p)}))\| - \|P_{\Sigma, \Sigma_{o_i}}(pre(s, \sigma^{(p)}))\| \leq k_i,$$

- ▶ **C3.** For all $\sigma_s \in \Sigma_{o,i}^s$, if $\sigma_s^{(p)} \in s_a$ then

$$(\sigma^{(p)} \in pre(s_a, \sigma_s^{(p)})) \wedge$$

$$(\|P_{\Sigma_a, \Sigma_{o_i}^s}(pre(s_a, \sigma_s^{(p)}))\| = \|P_{\Sigma, \Sigma_{o_i}}(pre(s, \sigma^{(p)}))\|)$$

The extension of χ to the domain 2^{Σ^*} is $\chi(L) := \bigcup_{t \in L} \chi_i(t)$.

Network diagnosability



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Network diagnosability



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Definition: Language $L(G)$ is network diagnosable with respect to augmentation $\chi : 2^{\Sigma^*} \rightarrow 2^{\Sigma_a^*}$, projection $P_{\Sigma_a, \Sigma_o^s} : \Sigma_a^* \rightarrow \Sigma_o^{s*}$ and $\Sigma_f = \{\sigma_f\}$ if the following holds true:

$$(\exists n \in \mathbb{N})(\forall s \in \Psi(\Sigma_f))(\forall t \in L/s)(\|t\| \geq n \Rightarrow N_D)$$

where the network diagnosability condition N_D is

$$(\nexists w \in L) [P_{\Sigma_a, \Sigma_o^s}(\chi(st)) \cap P_{\Sigma_a, \Sigma_o^s}(\chi(w)) \neq \emptyset \wedge (\Sigma_f \notin w)].$$

Verification of Network diagnosability

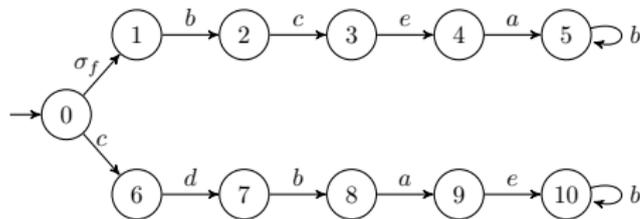
- ▶ **Basic idea:** construct an augmented automaton G_a such that $L(G_a) = \chi(L(G))$

Verification of Network diagnosability

- ▶ **Basic idea:** construct an augmented automaton G_a such that $L(G_a) = \chi(L(G))$
- ▶ **Alves et al., (2021)** proposes a construction for $G_a = (X_a, \Sigma_a, \delta_a, x_{a_0})$, whose general idea is as follows:
 - ▶ $x_a = (x, q)$
 - ✓ x is the current state of G
 - ✓ $q = \sigma_1 n_1 \sigma_1 n_2 \dots \sigma_p n_p$
 - where
 - ✓ $\sigma_j \in \Sigma_o$: event occurrence
 - ✓ n_j : counts the number of event occurrences (observable or unobservable) after the occurrence of σ_j
 - ▶ $x_a = (5, c2a0)$
 - ✓ G is currently at 5 and ✓ either one unobservable event has occurred between the occurrences of c and a , ✓ or one observable event has occurred and its transmission has been successfully received at the diagnoser.

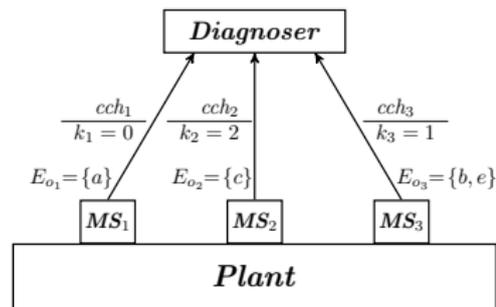
Back to the Motivation Example of Networked DES

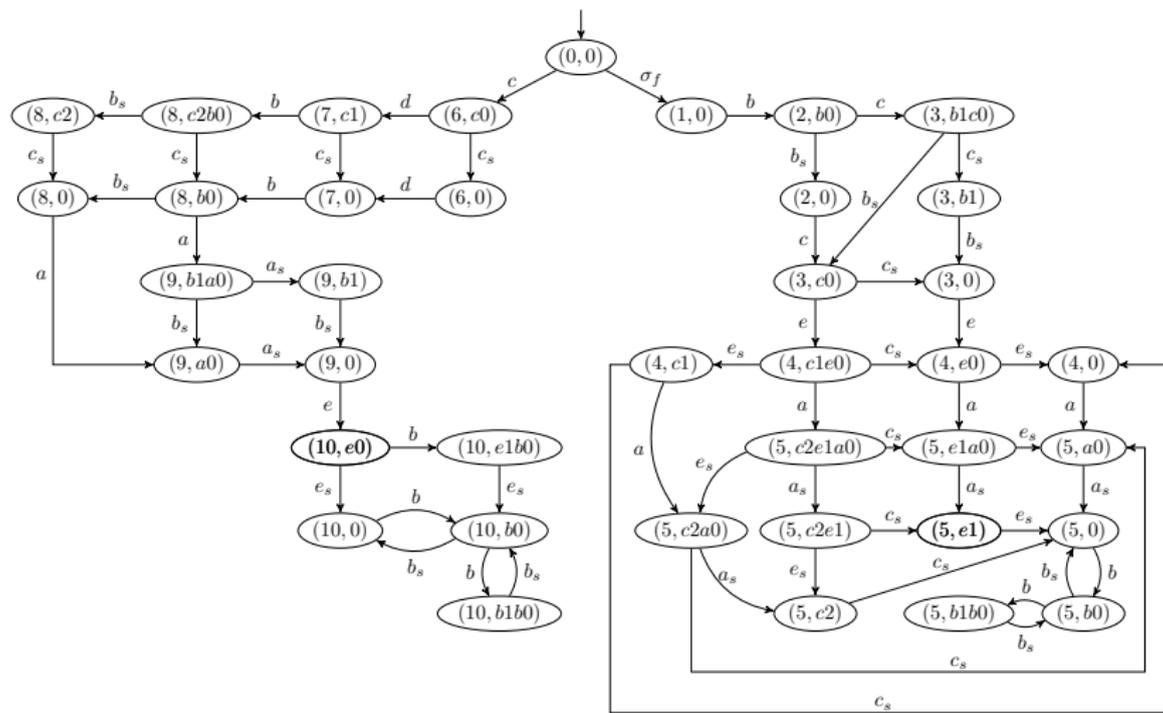
▶ Automaton



- ▶ $\Sigma = \{a, b, c, d, e, \sigma_f\}$, $\Sigma_f = \{\sigma_f\}$
- ▶ $\Sigma_o^s = \{a_s, b_s, c_s, e_s\}$
- ▶ $\vec{k} = [0 \ 2 \ 1]$

▶ Networked DES



Augmented automaton G_a 

Verification of network diagnosability

- ▶ It can be performed with any verification algorithm applied on G_a assuming Σ_o^s as the set of observable events (Moreira et al., 2012, Viana & Basilio, 2019)

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- ▶ Loss of observation can also be taken into account by applying dilation to events $\sigma_s \in \Sigma_o^s$ that are subject to intermittent loss of observation
- ▶ $L(G)$ is not network diagnosable with respect to χ , P_{Σ_a, Σ_o^s} and σ_f .

VII. Conclusion



Concluding remarks

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Concluding remarks

- ▶ We have restricted ourselves to the problem of diagnosability and diagnosis of monolithic DES
- ▶ When the physical system has a distributed structure, it is more appropriate to consider the decentralized diagnosability notions proposed in [Debouk et al. \(2000\)](#) and [Contant et al. \(2002\)](#)
- ▶ Indeed, robust diagnosability was introduced in the DES community for decentralized DES ([Basilio and Lafortune, 2009](#))

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- ▶ The augmentation approach adopted in the diagnosability of networked DES can be leveraged so as to allow other problems of networked DES, such as networked supervisory control or opacity enforcement, to be converted in standard problems, which can be solved with existing tools.

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- ▶ The augmentation approach adopted in the diagnosability of networked DES can be leveraged so as to allow other problems of networked DES, such as networked supervisory control or opacity enforcement, to be converted in standard problems, which can be solved with existing tools.
- ▶ Robust diagnosis of DES is a lively research topic. There is still much to be done!

Acknowledgments

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